

1-4 Practice

Name the property that each statement illustrates.

1. $12 + 917 = 917 + 12$

2. $74.5 \cdot 0 = 0$

3. $35 \cdot x = x \cdot 35$

4. $3 \cdot (-1 \cdot p) = 3 \cdot (-p)$

5. $m + 0 = m$

6. $53.7 \cdot 1 = 53.7$

Use mental math to simplify each expression.

7. $36 + 12 + 4$

8. $19.2 + 0.6 + 12.4 + 0.8$

9. $2 \cdot 16 \cdot 10 \cdot 5$

10. $12 \cdot 18 \cdot 0 \cdot 17$

Simplify each expression. Justify each step.

11. $6 + (8x + 12)$

12. $5(16p)$

13. $(2 + 7m) + 5$

14.
$$\frac{12st}{4t}$$

Tell whether the expressions in each pair are equivalent.

15. $7x$ and $7x \cdot 1$

16. $4 + 6 + x$ and $4 \cdot x \cdot 6$

17. $(12 - 7) + x$ and $5x$

18. $p(4 - 4)$ and 0

19.
$$\frac{24xy}{2x}$$
 and $12y$

20.
$$\frac{27m}{(3+9-12)}$$
 and $27m$

21. You have prepared 42 mL of distilled water, 18 mL of vinegar and 47 mL of salt water for an experiment.

- How many milliliters of solution will you have if you first pour the distilled water, then the salt water, and finally the vinegar into your beaker?
- How many milliliters of solution will you have if you first pour the salt water, then the vinegar, and finally the distilled water into your beaker?
- Explain why the amounts described in parts (a) and (b) are equal.

1-4 Practice (continued)

Use deductive reasoning to tell whether each statement is *true* or *false*. If it is false, give a counterexample.

22. For all real numbers a and b , $a - b = -b + a$.

23. For all real numbers p , q and r , $p - q - r = p - r - q$.

24. For all real numbers x , y and z , $(x + y) + z = z + (x + y)$.

25. For all real numbers m and n , $\frac{m}{n} \cdot n = \frac{n}{m} \cdot m$.

26. **Writing** Explain why the commutative and associative properties don't hold true for subtraction and division but the identity properties do.

27. **Reasoning** A recipe for brownies calls for mixing one cup of sugar with two cups of flour and 4 ounces of chocolate. They are all to be mixed in a bowl before baking. Will the brownies taste different if you add the ingredients in different orders? Relate your answer to a property of real numbers.

Simplify each expression. Justify each step.

28. $(6^7)(5^3 + 2)(2 - 2)$

29. $(m - 16)(-7 \div -7)$

30. **Open-Ended** Provide examples to show the following.

- a. The associative property of addition holds true for negative integers.
- b. The commutative property of multiplication holds true for non-integers.
- c. The multiplicative property of negative one holds true regardless of the sign of the number on which the operation is performed.
- d. The commutative property of multiplication holds true if one of the factors is zero.